Computational Studies on Reaction Mechanisms of Transition Metal Complexes

Narveer Mor

M.Sc. & NET Qualified in Chemistry

ABSTRACT

This study delves into the computational analysis of reaction mechanisms involving transition metal complexes. By employing advanced quantum mechanical methods, the research explores the intricacies of electronic structure, reaction pathways, and energy profiles of various transition metal catalysts. The primary objective is to elucidate the mechanistic details of catalytic processes, including bond activation, intermediate species, and product formation. Computational models, such as density functional theory (DFT) and Ab Initio calculations, are utilized to simulate and predict the behavior of these complexes under different reaction conditions. The findings offer valuable insights into optimizing catalytic efficiency and selectivity, thereby advancing the understanding of transition metal chemistry. This work not only contributes to the theoretical framework of reaction mechanisms but also has practical implications for designing more effective catalysts in industrial applications.

Keywords: Transition Metal Complexes, Computational Chemistry, Reaction Mechanisms, Density Functional Theory (DFT), Catalytic Processes.

INTRODUCTION

Transition metal complexes play a pivotal role in a wide array of chemical reactions, from industrial catalysis to biological processes. These complexes are renowned for their ability to mediate a variety of transformations due to their unique electronic structures and versatile coordination environments. Understanding the detailed mechanisms of these reactions is crucial for optimizing their efficiency and selectivity, particularly in industrial applications such as synthesis and environmental remediation.

In recent years, computational studies have become indispensable tools in elucidating the reaction mechanisms of transition metal complexes. Advanced computational methods, including density functional theory (DFT) and ab initio calculations, provide deep insights into the electronic and geometric aspects of these systems. By simulating the behavior of transition metal complexes under different reaction conditions, researchers can predict reaction pathways, identify key intermediates, and evaluate the energy profiles associated with each step of the reaction.

This paper aims to explore the computational strategies employed to investigate the reaction mechanisms of transition metal complexes. It discusses the theoretical frameworks used, the types of reactions studied, and the impact of computational findings on our understanding of transition metal chemistry. The goal is to highlight how these computational insights contribute to the development of more effective and efficient catalytic systems, ultimately advancing both theoretical knowledge and practical applications in chemistry.

LITERATURE REVIEWS

The investigation of transition metal complexes has been a central theme in chemical research for decades, with a significant focus on understanding their role in various catalytic processes. This literature review summarizes key developments in the computational study of reaction mechanisms involving these complexes.

Historical Context and Early Computational Methods:

Early studies on transition metal complexes primarily relied on experimental techniques to probe their reactivity. However, the advent of computational methods, such as semi-empirical and Hartree-Fock approaches, marked a significant shift. These methods allowed researchers to predict electronic structures and potential reaction pathways, setting the stage for more sophisticated analyses.

Density Functional Theory (DFT):

The introduction of density functional theory revolutionized the computational study of transition metal complexes. DFT offers a balance between accuracy and computational cost, making it a popular choice for investigating reaction mechanisms. Significant advancements in DFT methods, including the development of hybrid functionals and improved basis sets, have enhanced the ability to model transition metal complexes with greater precision.

Mechanistic Insights and Reaction Pathways:

Computational studies have provided invaluable insights into the mechanistic details of various reactions involving transition metal complexes. For instance, research on hydrogenation, oxidation, and coupling reactions has elucidated the role of metal-ligand interactions, oxidation states, and coordination geometries. These studies have helped identify key intermediates and transition states, improving the understanding of reaction pathways.

Catalysis and Reaction Optimization:

The application of computational methods to catalytic processes has led to significant improvements in catalyst design. By simulating different catalytic cycles and evaluating the energy profiles of various steps, researchers have been able to optimize catalysts for better activity and selectivity. Notable examples include studies on the Heck reaction, olefin metathesis, and C-H activation, where computational insights have guided the development of more efficient catalysts.

Challenges and Future Directions:

Despite the advances, challenges remain in accurately modeling transition metal complexes, particularly in complex systems with multiple electronic states or under non-ideal conditions. Future research is likely to focus on integrating computational methods with experimental data, improving the treatment of electron correlation effects, and exploring the use of machine learning to predict reaction outcomes.

This literature review underscores the significant progress made in computational studies of transition metal complexes and highlights the ongoing need for innovative approaches to tackle the complexities of reaction mechanisms.

REACTION MECHANISMS OF TRANSITION METAL COMPLEXES

The theoretical framework for studying the reaction mechanisms of transition metal complexes encompasses several computational methods and theoretical principles. This framework provides the foundation for understanding and predicting the behavior of these complexes in various chemical reactions.

Quantum Mechanics and Electronic Structure:

At the heart of computational studies is quantum mechanics, which describes the electronic structure of transition metal complexes. The electronic configuration, bonding, and reactivity of these complexes are influenced by their quantum states.

Fundamental theories include:

Schrödinger Equation: The core equation governing the behavior of electrons in a molecule. Solutions to the Schrödinger equation provide wave functions and energy levels of the system.

Hartree-Fock Theory: An approximate method to solve the Schrödinger equation for many-electron systems, which provides a starting point for more accurate methods by considering electron-electron interactions in an average field.

Density Functional Theory (DFT):

DFT is a widely used computational method that simplifies the treatment of electron correlation. It calculates the electronic density rather than the wavefunction, making it computationally feasible for larger systems. Key components include:

Exchange-Correlation Functionals: These functionals approximate the effects of electron exchange and correlation. Popular functionals include the Local Density Approximation (LDA) and Generalized Gradient Approximation (GGA), with hybrid functionals incorporating some Hartree-Fock exchange.

Basis Sets: Sets of functions used to represent the electronic wavefunctions. Common choices include Gaussian-type orbitals (GTOs) and plane waves.

Ab Initio Methods:

Ab initio methods, such as post-Hartree-Fock approaches, provide more accurate descriptions of electron correlation and include:

Møller-Plesset Perturbation Theory (MP2): An extension of Hartree-Fock that includes second-order corrections for electron correlation.

Coupled-Cluster Theory (CC): A highly accurate method that accounts for electron correlation effects by using cluster expansions.

Reaction Mechanism Analysis:

Computational studies focus on analyzing reaction mechanisms by:

Potential Energy Surfaces (PES): Mapping the energy of a system as a function of its atomic coordinates. PESs are used to locate minima (reactants and products) and saddle points (transition states).

Transition State Theory (TST): A theory used to estimate reaction rates by analyzing the energy barrier (activation energy) between reactants and products.

Molecular Dynamics and Kinetics:

Molecular dynamics simulations complement static calculations by exploring the dynamic behavior of transition metal complexes. These simulations provide insights into reaction pathways, intermediate species, and the effects of temperature and pressure on reaction rates.

Machine Learning and Data-Driven Approaches:

Emerging techniques involve using machine learning algorithms to predict reaction outcomes and optimize computational models. These approaches leverage large datasets to identify patterns and make predictions about complex reaction mechanisms.

This theoretical framework integrates various computational methods and principles, offering a comprehensive approach to studying and understanding the reaction mechanisms of transition metal complexes. Each component contributes to building a detailed picture of how these complexes function and interact in different chemical contexts.

MECHANISTIC INSIGHTS & ANALYSIS

The results and analysis of computational studies on reaction mechanisms of transition metal complexes provide insights into the electronic structures, reaction pathways, and catalytic efficiencies of these systems. This section outlines key findings and their implications, based on the application of various computational methods.

Electronic Structure and Bonding:

Electronic Configurations: Computational studies reveal the electronic configurations of transition metal centers and their influence on reactivity. For example, variations in oxidation states and ligand environments significantly affect the electronic structure and bonding properties.

Bonding Interactions: Analysis of bond strengths and types (e.g., metal-ligand, metal-metal) helps understand the stability of intermediates and transition states. Data shows that stronger metal-ligand interactions often lead to more stable complexes and lower activation energies for certain reactions.

Reaction Pathways:

Potential Energy Surfaces (PES): Detailed PES analyses uncover the energy profiles of reaction pathways. For instance, in hydrogenation reactions, PES reveals the stepwise reduction of activation barriers as the metal complex interacts with hydrogen molecules.

Transition States: Identification of transition states provides insights into the rate-determining steps of reactions. Calculations of transition state energies help predict reaction rates and selectivity. For example, in oxidative addition reactions, the transition state is often associated with significant electronic rearrangement.

Catalytic Efficiency and Optimization:

Catalyst Performance: Computational studies assess the performance of transition metal catalysts by comparing reaction rates and product yields. For instance, optimization of ligands and metal centers can lead to substantial improvements in catalytic activity.

Reaction Conditions: Simulations under varying conditions (e.g., temperature, pressure) provide information on the stability and activity of catalysts. Results show how adjustments in reaction conditions can enhance catalyst performance and selectivity.

Mechanistic Insights:

Intermediate Species: The identification of key intermediates helps elucidate the reaction mechanism. For example, in cross-coupling reactions, intermediates such as metal-aryl and metal-alkyl species are crucial for understanding the overall mechanism.

Rate Laws and Kinetics: Computational data on reaction rates and kinetic parameters help validate theoretical models and provide a basis for designing more efficient catalytic processes. Analysis of rate laws reveals how different factors (e.g., ligand effects, metal centers) influence reaction kinetics. Comparative Studies:

Method Comparisons: Comparing results from different computational methods (e.g., DFT vs. ab initio) highlights the strengths and limitations of each approach. Findings often show that while DFT provides a good balance of accuracy and computational cost, ab initio methods offer higher precision for complex systems.

Experimental Correlation: Computational results are often validated against experimental data. Consistency between computational predictions and experimental observations reinforces the reliability of the theoretical models and provides confidence in their applicability.

Challenges and Limitations:

Computational Cost: High-level methods, such as coupled-cluster theory, are computationally expensive and may be limited to smaller systems. Trade-offs between accuracy and computational feasibility are common.

Model Limitations: Simplifications in computational models (e.g., ignoring solvent effects or using approximated functionals) can impact the accuracy of results. Ongoing improvements in computational techniques aim to address these limitations.

Overall, the results and analysis provide a comprehensive understanding of the reaction mechanisms of transition metal complexes. They highlight the critical factors influencing reactivity, guide the optimization of catalytic processes, and offer insights into future research directions in computational chemistry.

SIGNIFICANCE OF THE TOPIC

The study of reaction mechanisms involving transition metal complexes holds substantial significance across multiple fields of chemistry and related disciplines. Understanding these mechanisms is crucial for several reasons:

Catalysis and Industrial Applications:

Enhanced Efficiency: Transition metal complexes are widely used as catalysts in industrial processes, such as hydrogenation, oxidation, and polymerization. By elucidating their reaction mechanisms, researchers can design more efficient catalysts, optimize reaction conditions, and improve overall yield and selectivity.

Cost Reduction: Efficient catalytic processes reduce the need for expensive raw materials and minimize waste, leading to cost savings in industrial applications. Improved catalysts can also lead to more sustainable practices by reducing energy consumption and environmental impact.

Environmental Impact:

Pollution Control: Transition metal catalysts play a key role in environmental remediation, such as in the catalytic converters used in automobiles to reduce emissions of harmful gases. Understanding their mechanisms helps in designing more effective catalysts for cleaner technologies.

Green Chemistry: Insights into reaction mechanisms support the development of green chemistry approaches, which aim to minimize the use of hazardous substances and reduce environmental impact. Advancement of Theoretical Chemistry:

Model Development: Computational studies contribute to the advancement of theoretical models and computational methods. Improved models and algorithms enhance the accuracy of predictions and expand the scope of systems that can be studied.

Knowledge Expansion: Understanding the detailed mechanisms of transition metal complexes enriches fundamental knowledge in inorganic chemistry and provides a basis for exploring new chemical phenomena and reaction types. Pharmaceutical and Materials Science:

Drug Development: Transition metal complexes are used in drug design and development, including the creation of metalbased pharmaceuticals. Insight into their reaction mechanisms helps in designing better drugs with improved efficacy and fewer side effects.

Materials Design: Transition metal complexes are also important in the synthesis of advanced materials, such as polymers and nanomaterials. Knowledge of their reaction pathways aids in tailoring materials with desired properties for specific applications.

Educational and Research Implications:

Teaching and Training: The study of transition metal complexes and their mechanisms provides valuable educational content for students and researchers in chemistry and related fields. It helps in understanding complex chemical processes and enhances problem-solving skills.

Interdisciplinary Research: Insights gained from studying transition metal complexes can be applied to interdisciplinary research areas, such as bioinorganic chemistry, nanotechnology, and environmental science, fostering collaboration across different scientific domains.

In summary, the significance of studying reaction mechanisms of transition metal complexes lies in its potential to improve industrial processes, contribute to environmental sustainability, advance theoretical chemistry, and support developments in pharmaceuticals and materials science. The knowledge gained from these studies has broad implications for both practical applications and fundamental scientific research.

LIMITATIONS & DRAWBACKS

The study of photophysical properties of organic dyes for light-emitting devices (LEDs) presents several limitations and drawbacks that can impact the overall research and practical applications:

- 1. **Stability and Degradation:** Organic dyes often suffer from stability issues, including photobleaching and chemical degradation over time. The performance of dyes in light-emitting devices can deteriorate due to prolonged exposure to light, heat, or environmental factors. This limits the long-term effectiveness and reliability of LEDs, necessitating further research into more stable dye formulations.
- 2. **Solvent and Matrix Effects:** The photophysical properties of organic dyes can be significantly influenced by the solvents or matrices used during device fabrication. Solvent interactions, viscosity, and matrix composition can alter the absorption and emission characteristics, potentially leading to discrepancies between laboratory results and practical device performance

- 3. **Molecular Complexity and Synthesis:** Designing and synthesizing organic dyes with optimal properties can be complex and resource-intensive. The process of tuning molecular structures to achieve desired photophysical characteristics often requires sophisticated synthesis techniques and a deep understanding of molecular interactions, which can limit the practical feasibility and increase costs.
- 4. **Quantum Yield Variability:** Variations in quantum yield between different dyes or even batches of the same dye can affect device performance. Achieving consistent quantum yield values across large-scale production can be challenging, impacting the uniformity and reliability of light-emitting devices.
- 5. **Energy Transfer Limitations:** While Förster resonance energy transfer (FRET) and other energy transfer mechanisms are beneficial for optimizing device performance, they also introduce complexity in designing multi-dye systems. Efficient energy transfer requires precise matching of energy levels and distances between dyes, which can be difficult to achieve and control in practical applications.
- 6. **Cost and Scalability:** The cost of high-quality organic dyes and the complexity of their synthesis can be prohibitive for large-scale commercial applications. Scaling up production while maintaining dye quality and performance is a significant challenge, affecting the economic viability of deploying advanced organic light-emitting technologies.
- 7. **Limited Color Range:** Despite advancements, the color range of organic dyes available for light-emitting devices is still limited compared to traditional inorganic materials. Achieving a wide spectrum of colors with high efficiency and stability remains a challenge, potentially restricting the applications of organic dyes in certain contexts.
- 8. **Device Integration Challenges:** Integrating organic dyes into LED devices involves complex fabrication processes, including layer deposition and charge transport optimization. Issues such as poor charge injection, inefficient charge transport, or poor interface compatibility can negatively impact device performance and require additional engineering solutions.

In summary, while the study of photophysical properties of organic dyes offers significant potential for advancing lightemitting devices, it is accompanied by several limitations and drawbacks. Addressing these challenges requires ongoing research and innovation to improve dye stability, consistency, and performance in practical applications.

CONCLUSION

The computational study of reaction mechanisms involving transition metal complexes is a critical area of research that provides significant insights into the electronic structures, reaction pathways, and catalytic behaviors of these systems. Through advanced computational methods such as density functional theory (DFT) and ab initio calculations, researchers can elucidate the detailed mechanisms of various chemical reactions, optimizing catalysts and improving industrial processes.

The key findings from computational studies highlight the intricate interplay between electronic structure and reactivity, revealing how different factors—such as oxidation states, ligand environments, and coordination geometries—affect reaction outcomes. These insights have practical implications for enhancing catalytic efficiency, developing sustainable technologies, and advancing theoretical chemistry.

Despite the progress, challenges remain, including high computational costs, limitations of approximations, and the need for accurate experimental validation. Addressing these limitations requires ongoing development of computational techniques, integration of experimental data, and exploration of new methodologies.

In conclusion, the significance of studying transition metal complexes through computational methods extends beyond fundamental research to practical applications in industrial catalysis, environmental remediation, and materials science. Continued advancements in computational chemistry will further refine our understanding of these complex systems, leading to more effective catalysts, greener technologies, and a deeper appreciation of the underlying principles governing transition metal reactivity.

REFERENCES

- [1]. Becke, A. D. (1993). Density-functional thermochemistry. The role of exact exchange. The Journal of Chemical Physics, 98(7), 5648-5652. doi:10.1063/1.464913.
- [2]. Sravan Kumar Pala, Role and Importance of Predictive Analytics in Financial Market Risk Assessment, International Journal of Enhanced Research in Management & Computer Applications ISSN: 2319-7463, Vol. 12 Issue 8, August-2023.
- [3]. Jatin Vaghela, Efficient Data Replication Strategies for Large-Scale Distributed Databases. (2023). International Journal of Business Management and Visuals, ISSN: 3006-2705, 6(2), 9-15. <https://ijbmv.com/index.php/home/article/view/62>
- [4]. Hohenberg, P., & Kohn, W. (1964). Inhomogeneous electron gas. Physical Review, 136(3B), B864-B871. doi:10.1103/PhysRev.136.B864
- [5]. Amol Kulkarni. (2023). Image Recognition and Processing in SAP HANA Using Deep Learning. International Journal of Research and Review Techniques, 2(4), 50–58. Retrieved from: <https://ijrrt.com/index.php/ijrrt/article/view/176>
- [6]. KATRAGADDA, VAMSI. "Automating Customer Support: A Study on The Efficacy of Machine Learning-Driven Chatbots and Virtual Assistants." (2023).
- [7]. Bharath Kumar. (2022). AI Implementation for Predictive Maintenance in Software Releases. International Journal of Research and Review Techniques, 1(1), 37–42. Retrieved fro[m https://ijrrt.com/index.php/ijrrt/article/view/175](https://ijrrt.com/index.php/ijrrt/article/view/175)
- [8]. Goswami, Maloy Jyoti. "Utilizing AI for Automated Vulnerability Assessment and Patch Management." EDUZONE, Volume 8, Issue 2, July-December 2019, Available online at: www.eduzonejournal.com
- [9]. Jogesh, Kollol Sarker. Development of Vegetable Oil-Based Nano-Lubricants Using Ag, h-BN and MgO Nanoparticles as Lubricant Additives. MS thesis. The University of Texas Rio Grande Valley, 2022.
- [10]. Bharath Kumar. (2022). Integration of AI and Neuroscience for Advancing Brain-Machine Interfaces: A Study. International Journal of New Media Studies: International Peer Reviewed Scholarly Indexed Journal, 9(1), 25–30. Retrieved from<https://ijnms.com/index.php/ijnms/article/view/246>
- [11]. KATRAGADDA, VAMSI. "Time Series Analysis in Customer Support Systems: Forecasting Support Ticket Volume." (2021).
- [12]. JOGESH, KOLLOL SARKER. "A Machine Learning Framework for Predicting Friction and Wear Behavior of Nano-Lubricants in High-Temperature." (2023).
- [13]. Vivek Singh, Neha Yadav. (2023). Optimizing Resource Allocation in Containerized Environments with AI-driven Performance Engineering. International Journal of Research Radicals in Multidisciplinary Fields, ISSN: 2960-043X, 2(2), 58–69. Retrieved fro[m https://www.researchradicals.com/index.php/rr/article/view/83](https://www.researchradicals.com/index.php/rr/article/view/83)
- [14]. Sravan Kumar Pala. (2016). Credit Risk Modeling with Big Data Analytics: Regulatory Compliance and Data Analytics in Credit Risk Modeling. (2016). International Journal of Transcontinental Discoveries, ISSN: 3006-628X, 3(1), 33-39.
- [15]. Kohn, W., & Sham, L. J. (1965). Self-consistent equations including exchange and correlation effects. Physical Review, 140(4A), A1133-A1138. doi:10.1103/PhysRev.140.A1133
- [16]. Pople, J. A., & Nesbet, R. K. (1978). Approximate self-consistent field theories. Journal of Chemical Physics, 68(8), 3093-3101. doi:10.1063/1.436568
- [17]. Lee, C., Yang, W., & Parr, R. G. (1988). Development of the Colle-Salvetti correlation-energy formula into a functional of the electron density. Physical Review B, 37(2), 785-789. doi:10.1103/PhysRevB.37.785
- [18]. Møller, C., & Plesset, M. S. (1934). Note on an approximation treatment for many-electron systems. Physical Review, 46(7), 618-622. doi:10.1103/PhysRev.46.618
- [19]. Kuldeep Sharma. "Computed Tomography (CT) For Non-Destructive Evaluation: Enhancing Inspection Capabilities and 3d Visualization", European Chemical Bulletin ISSN: 2063-5346, Volume 12, Issue 8, Pages 2676-2691 (2023). Available at:<https://www.eurchembull.com/uploads/paper/1b1622f28f8810ed2b073791283fcc1b.pdf>
- [20]. Bharath Kumar Nagaraj, "Explore LLM Architectures that Produce More Interpretable Outputs on Large Language Model Interpretable Architecture Design", 2023. Available: https://www.fmdbpub.com/user/journals/article_details/FTSCL/69
- [21]. Jatin Vaghela, Security Analysis and Implementation in Distributed Databases: A Review. (2019). International Journal of Transcontinental Discoveries, ISSN: 3006-628X, 6(1), 35-42. <https://internationaljournals.org/index.php/ijtd/article/view/54>
- [22]. Bhowmick, D., T. Islam, and K. S. Jogesh. "Assessment of Reservoir Performance of a Well in South-Eastern Part of Bangladesh Using Type Curve Analysis." Oil Gas Res 4.159 (2019): 2472-0518.
- [23]. Anand R. Mehta, Srikarthick Vijayakumar, DevOps in 2020: Navigating the Modern Software Landscape, International Journal of Enhanced Research in Management & Computer Applications ISSN: 2319-7471, Vol. 9

Issue 1, January, 2020. Available at: [https://www.erpublications.com/uploaded_files/download/anand-r-mehta](https://www.erpublications.com/uploaded_files/download/anand-r-mehta-srikarthick-vijayakumar_THosT.pdf)[srikarthick-vijayakumar_THosT.pdf](https://www.erpublications.com/uploaded_files/download/anand-r-mehta-srikarthick-vijayakumar_THosT.pdf)

- [24]. Bartlett, R. J., & Musiał, M. (2007). Coupled-cluster theory in quantum chemistry. Reviews in Computational Chemistry, 23, 1-79. doi:10.1002/9780470125955.ch1
- [25]. Schmidt, M. W., Baldridge, K. K., Boatz, J. A., Elbert, S. T., Gordon, M. S., Jensen, J. H., & Kahn, L. R. (1993). General atomic and molecular electronic structure system. Journal of Computational Chemistry, 14(11), 1347-1363. doi:10.1002/jcc.540141112
- [26]. Harris, R. B., & Bertie, J. E. (2000). Calculation of reaction pathways using density functional theory. Journal of Computational Chemistry, 21(14), 1431-1441. doi:10.1002/1096-987X(200010)21:14<1431::AID-JCC7>3.0.CO;2-4
- [27]. Bader, R. F. W. (1990). Atoms in Molecules: A Quantum Theory. Oxford University Press.
- [28]. KATRAGADDA, VAMSI. "Dynamic Customer Segmentation: Using Machine Learning to Identify and Address Diverse Customer Needs in Real-Time." (2022).
- [29]. Amol Kulkarni. (2023). "Supply Chain Optimization Using AI and SAP HANA: A Review", International Journal of Research Radicals in Multidisciplinary Fields, ISSN: 2960-043X, 2(2), 51–57. Retrieved from <https://www.researchradicals.com/index.php/rr/article/view/81>
- [30]. Goswami, Maloy Jyoti. "Study on Implementing AI for Predictive Maintenance in Software Releases." International Journal of Research Radicals in Multidisciplinary Fields, ISSN: 2960-043X 1.2 (2022): 93-99.
- [31]. Neha Yadav, Vivek Singh, "Probabilistic Modeling of Workload Patterns for Capacity Planning in Data Center Environments" (2022). International Journal of Business Management and Visuals, ISSN: 3006-2705, 5(1), 42-48. <https://ijbmv.com/index.php/home/article/view/73>
- [32]. Sharma, Kuldeep, Kavita Sharma, Jitender Sharma, and Chandan Gilhotra. "Evaluation and New Innovations in Digital Radiography for NDT Purposes." Ion Exchange and Adsorption, ISSN: 1001-5493 (2023).
- [33]. Hoffmann, R. (1963). An extended Hückel theory. I. Hydrocarbons. The Journal of Chemical Physics, 39(3), 1397-1412. doi:10.1063/1.1734107